

The Roles of Structure Formation and Λ in Black Hole Universes

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Based on arXiv:1610.05635 (Class. Quant. Grav. 34 065009) and arXiv:1707.xxxxx

Also arXiv:1705.01892 (Gen. Rel. Grav. 49: 98)

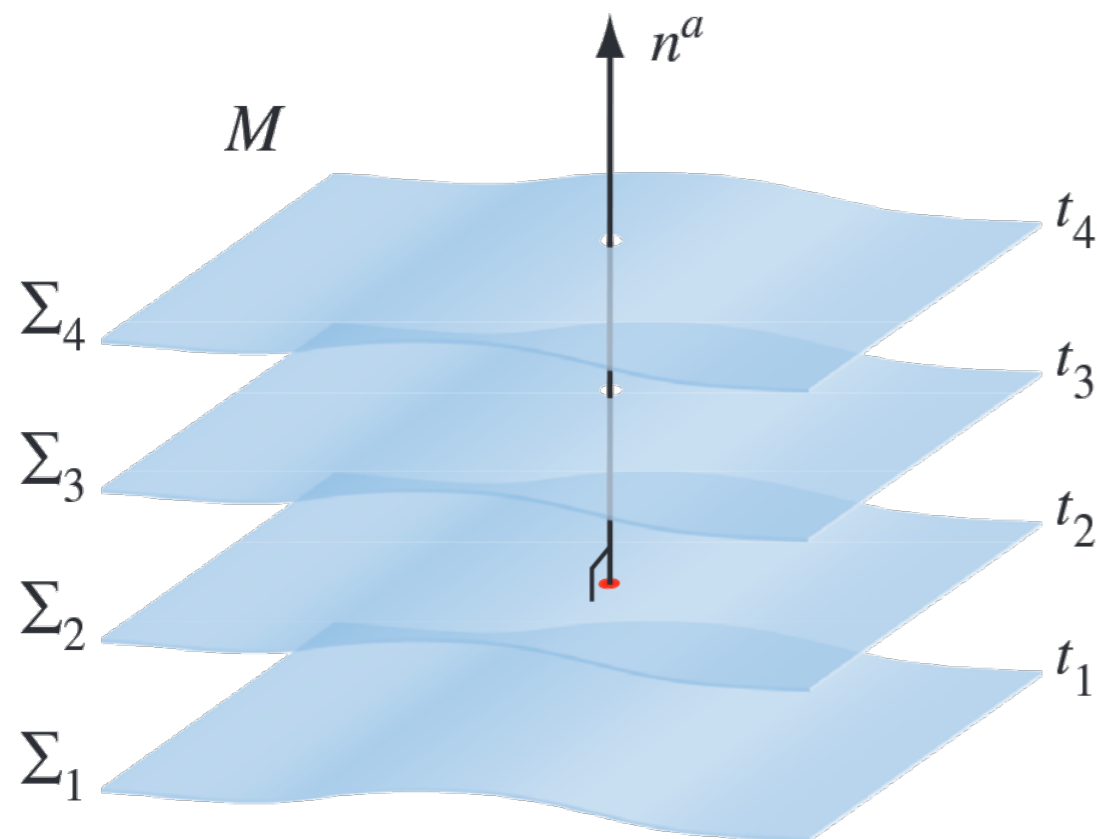
Motivation

Cosmological principle: homogeneous and isotropic. Wish to *test* whether large scale expansion of space is that of FLRW.

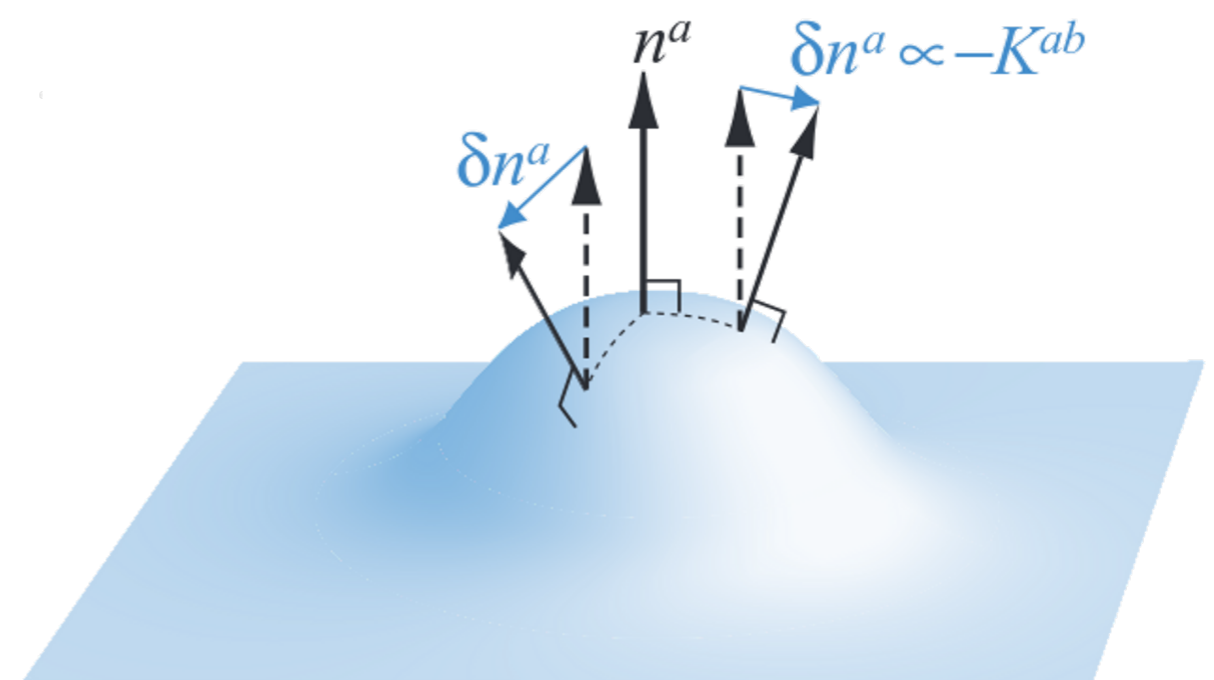
- **Theoretical:** \exists non-commutativity in EFE's \Rightarrow
 - small scale inhomogeneities may affect large scale dynamics (backreaction problem).
- **Observational:** homogeneity scale, effects on observables, precision cosmology.

Initial Data

- Full GR difficult to solve! Use 3 + 1 decomposition to instead get *constraint equations*, and specify the following:



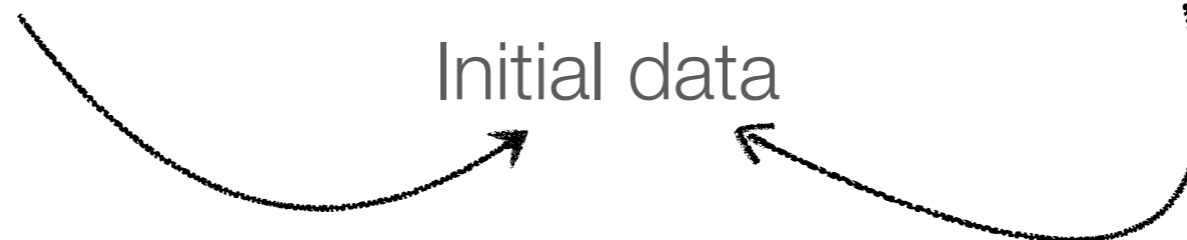
Hypersurface Σ_i , metric h_{ij}



Baumgarte & Shapiro,
Numerical Relativity (2010)

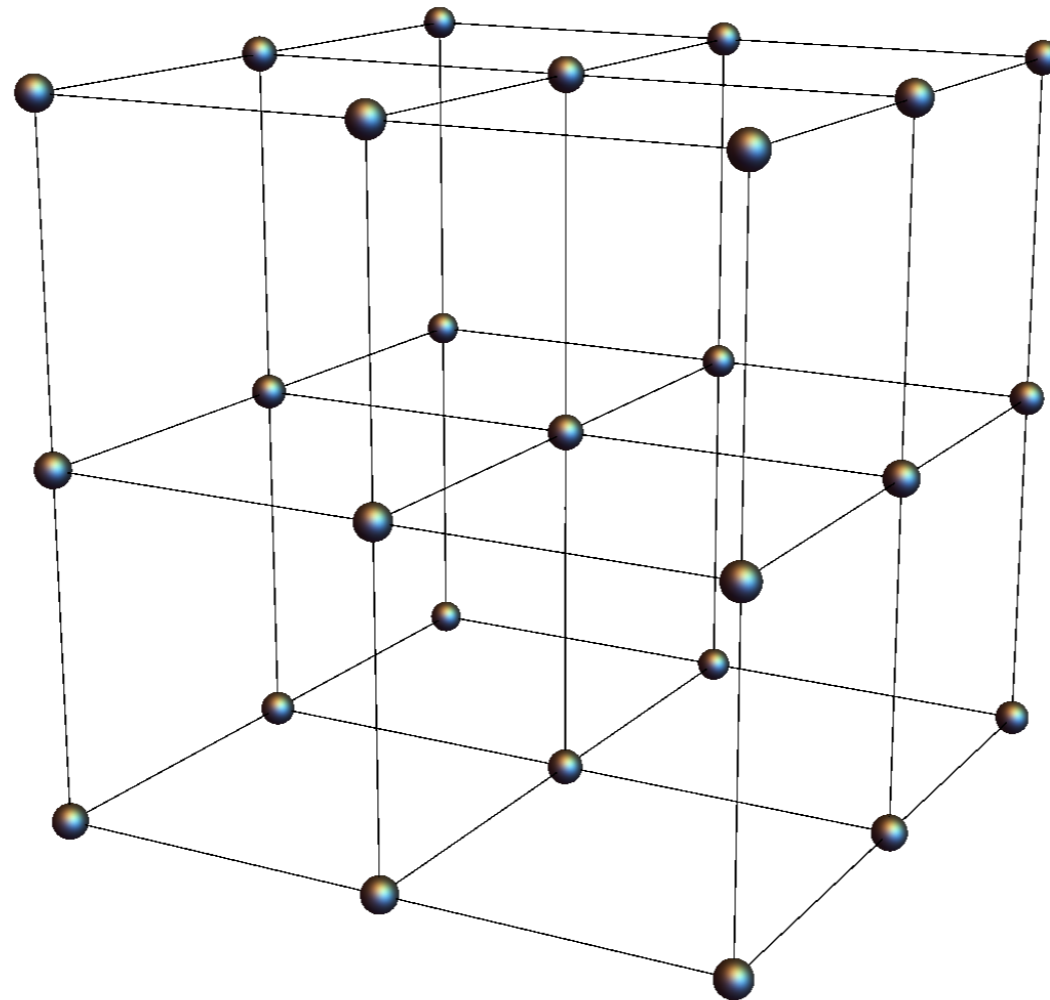
Extrinsic curvature $K_{\mu\nu}$

Initial data



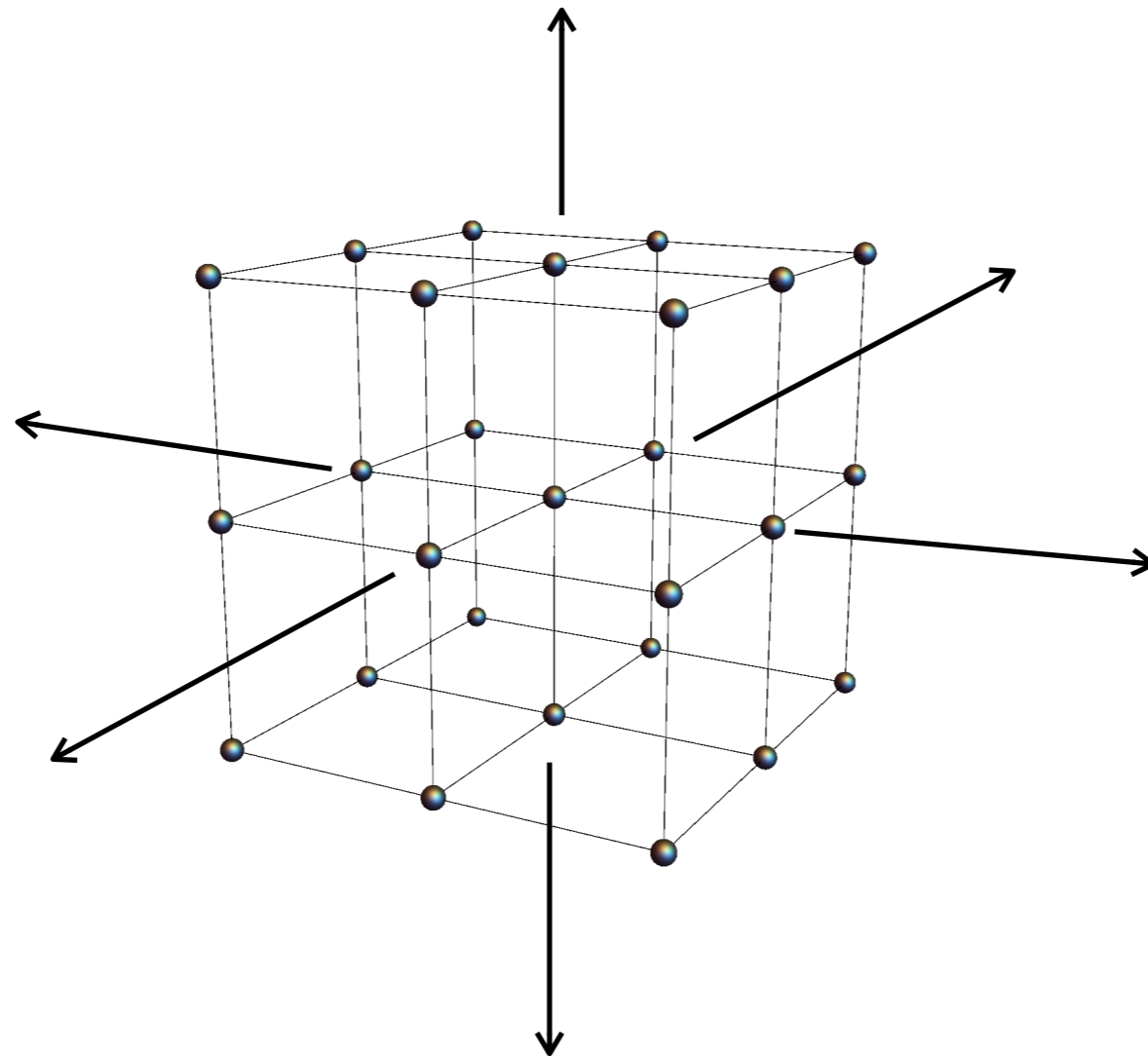
The Solution

- Exploit linearity that arises from conformally flat Schwarzschild solution. Superpose many Schwarzschild masses together - represents discretised matter content of Universe.



The Solution

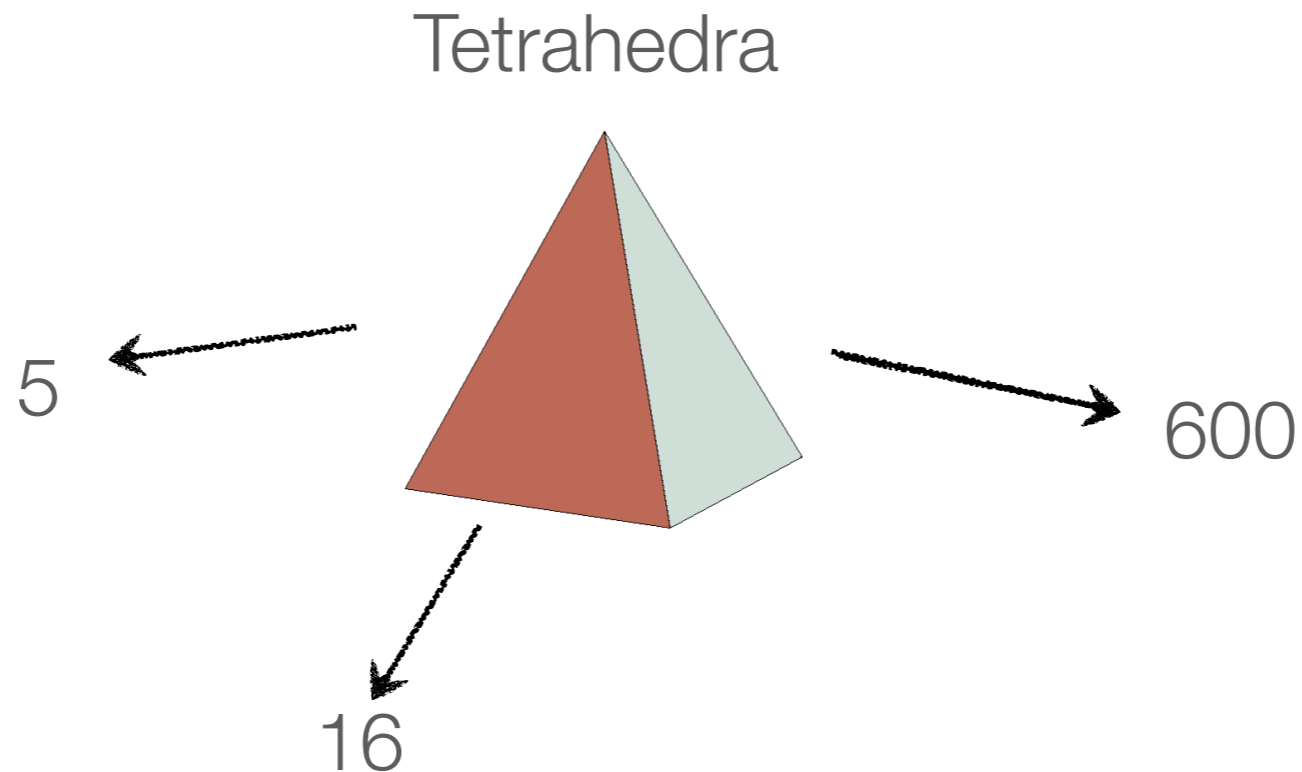
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The Solution

- NB: Want **exact** solutions. Tile 3-sphere with identical polyhedra, and place Schwarzschild mass at centre of each \therefore closed cosmological model. 6 ways of doing this:

>1 way to arrange:

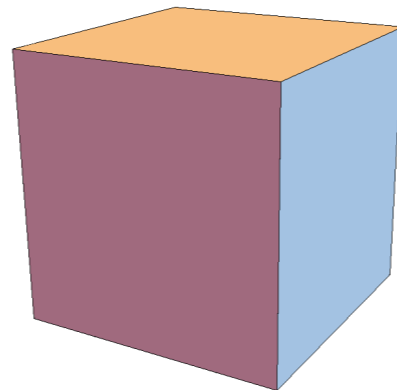


The Solution

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Only one way to arrange:

Cubes



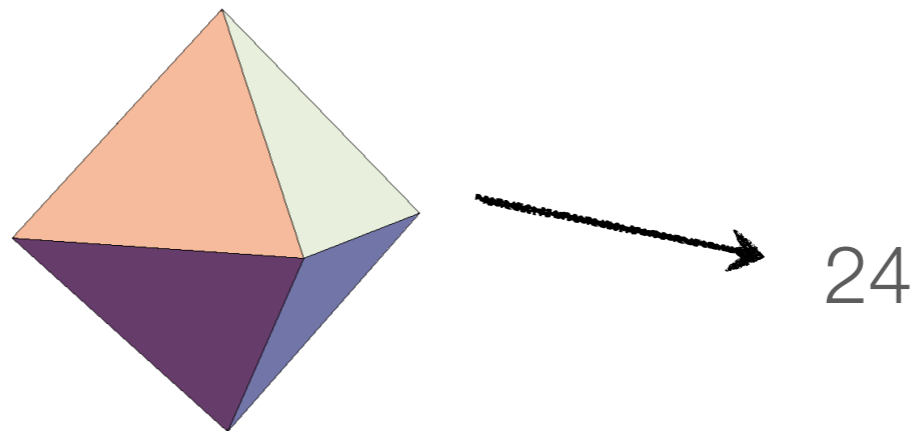
8

The Solution

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Only one way to arrange:

Octahedra

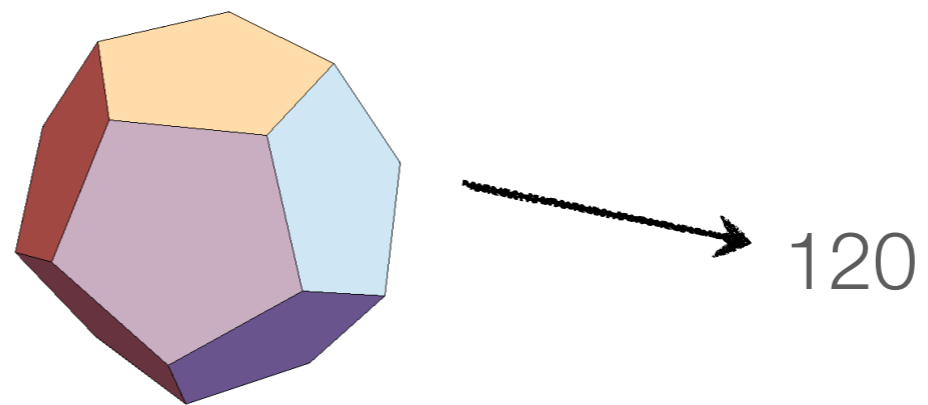


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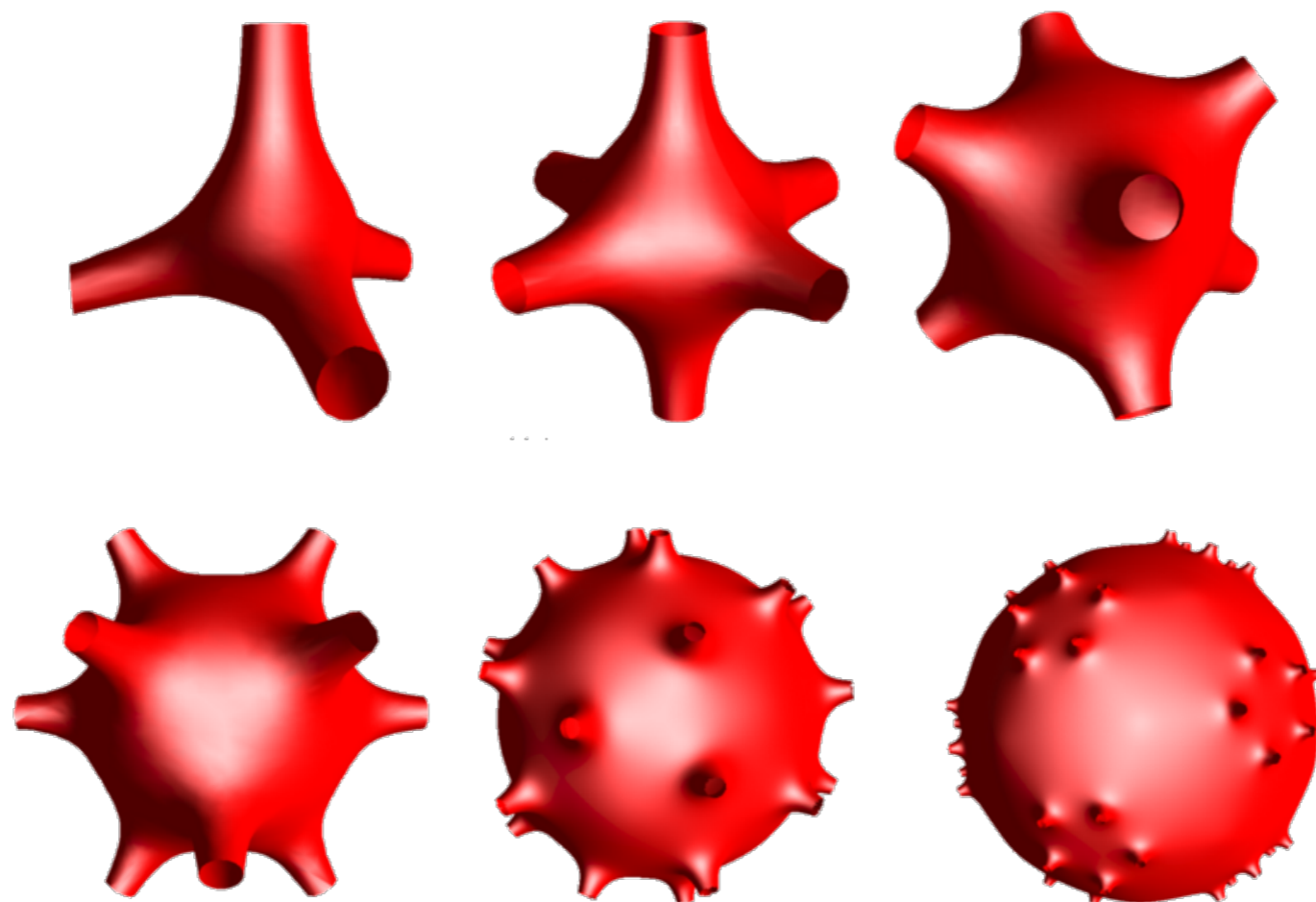
Only one way to arrange:

Dodecahedra



The Solution

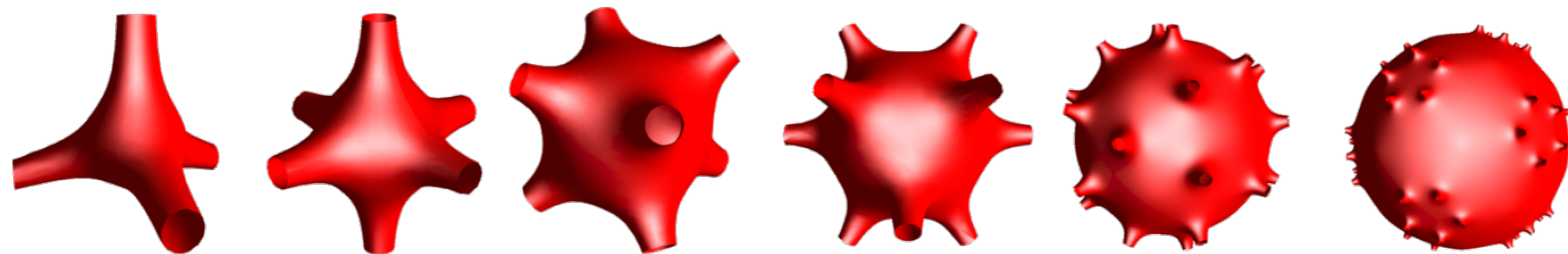
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Adding Λ

- Now looking at slice through Schwarzschild-de Sitter.
- $K_{\mu\nu}$ non-vanishing (no longer time symmetric).
- Appropriate choice: $K^2 = 3\Lambda$ to solve constraint eqⁿs.
 - \therefore looking at CMC foliation.

Intrinsic geometry identical to previous slice through Schwarzschild



Adding Λ

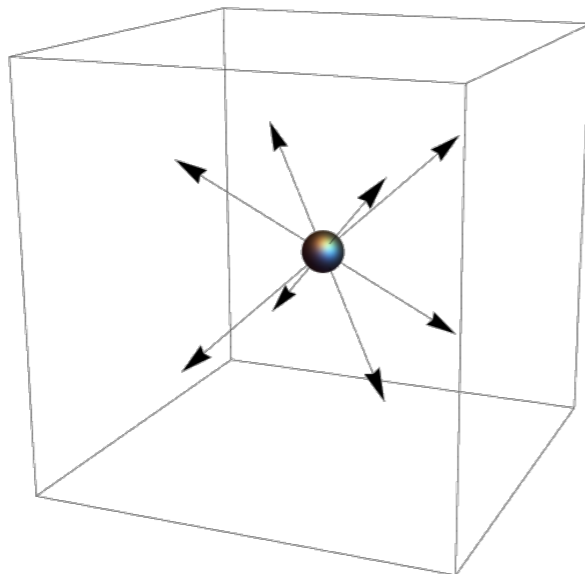
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Eternal expansion if $\Omega_\Lambda > 4/27 \Omega_m$.

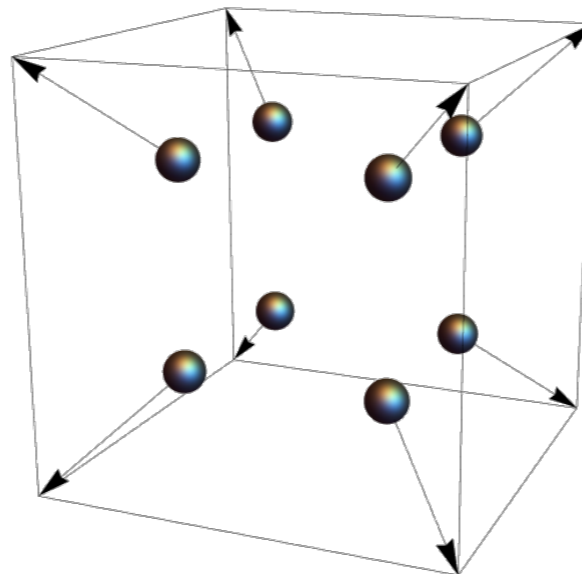
Adding Structure

- Split each mass at centre of cell into number of vertices of that cell, and move towards these vertices.

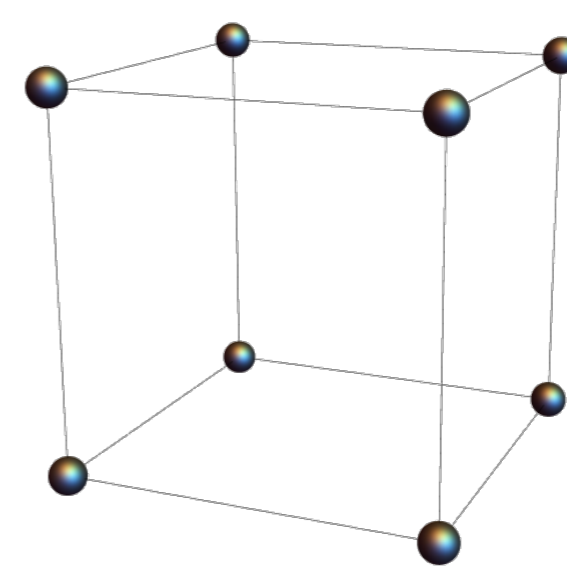
$$v(\lambda) = V_{\text{original}} + \lambda V_{\text{dual}} - \lambda V_{\text{original}}$$



(a) $\lambda = 0.$



(b) $\lambda = 0.5.$



(c) $\lambda = 1.$

Adding Structure

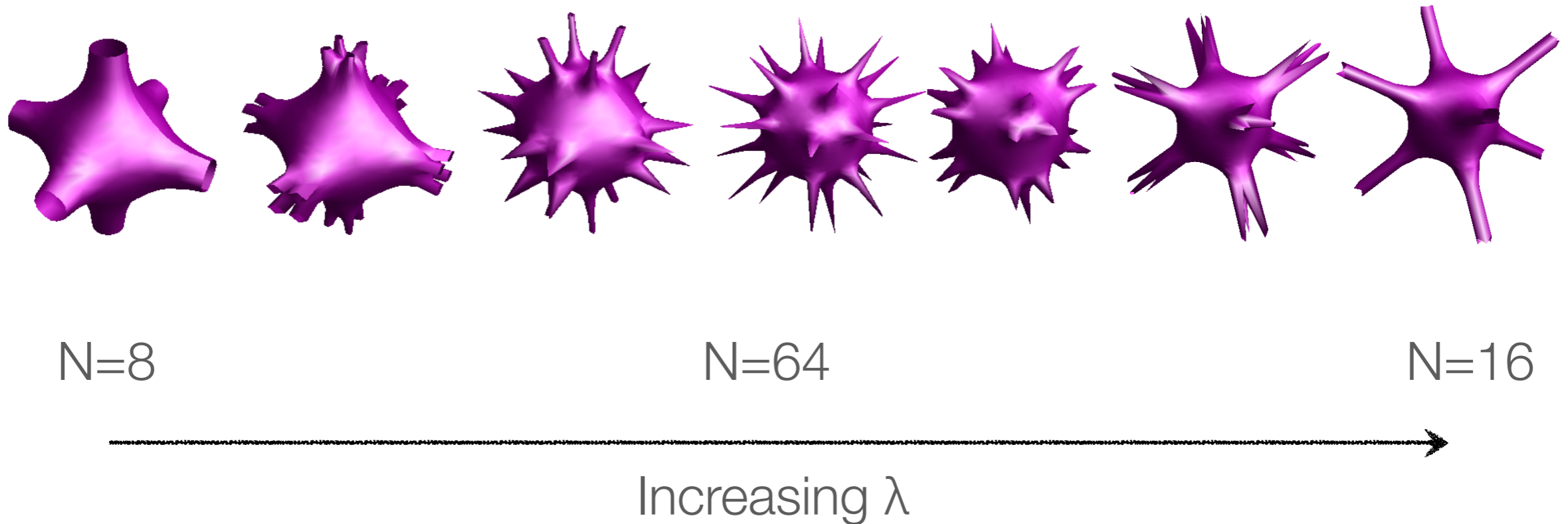
- Split each mass at centre of cell into number of vertices of that cell, and move towards these vertices.

| Original nº. | Cell shape | No. vertices | Total no. | Dual no. |
|--------------|--------------|--------------|-----------|----------|
| 5 | Tetrahedron | 4 | 20 | 5 |
| 8 | Cube | 8 | 64 | 16 |
| 16 | Tetrahedron | 4 | 64 | 8 |
| 24 | Octahedron | 6 | 144 | 24 |
| 120 | Dodecahedron | 20 | 2400 | 600 |
| 600 | Tetrahedron | 4 | 2400 | 120 |

Adding Structure

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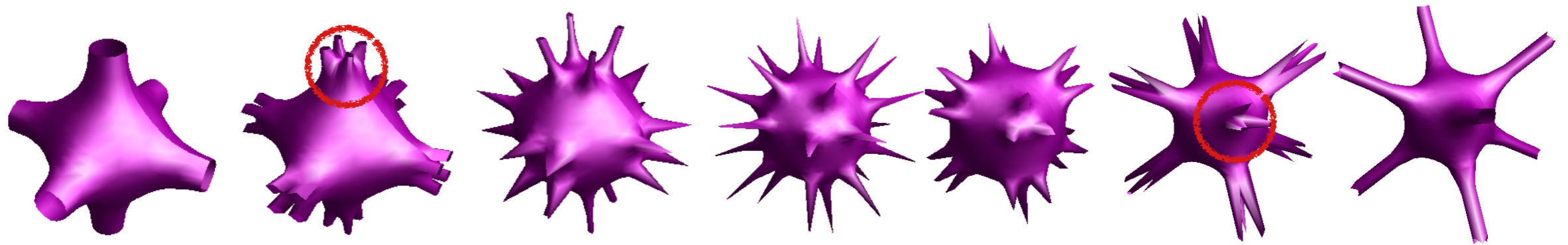
Intrinsic geometries now differ:



Adding Structure

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Intrinsic geometries now differ:



Structures...

Horizons

- Horizons are marginally trapped surfaces with vanishing expansion. Use electric part of Weyl tensor to locate.

Λ

Structure formation

Locating equation

$$\mathbf{e}_1(E^{11}) = \alpha_1 \alpha_2 (3\Lambda)^{1/2} E^{11}$$

$$\mathbf{e}_1(E^{11}) = 0$$

Type

Cosmological and black hole

Individual and collective black hole

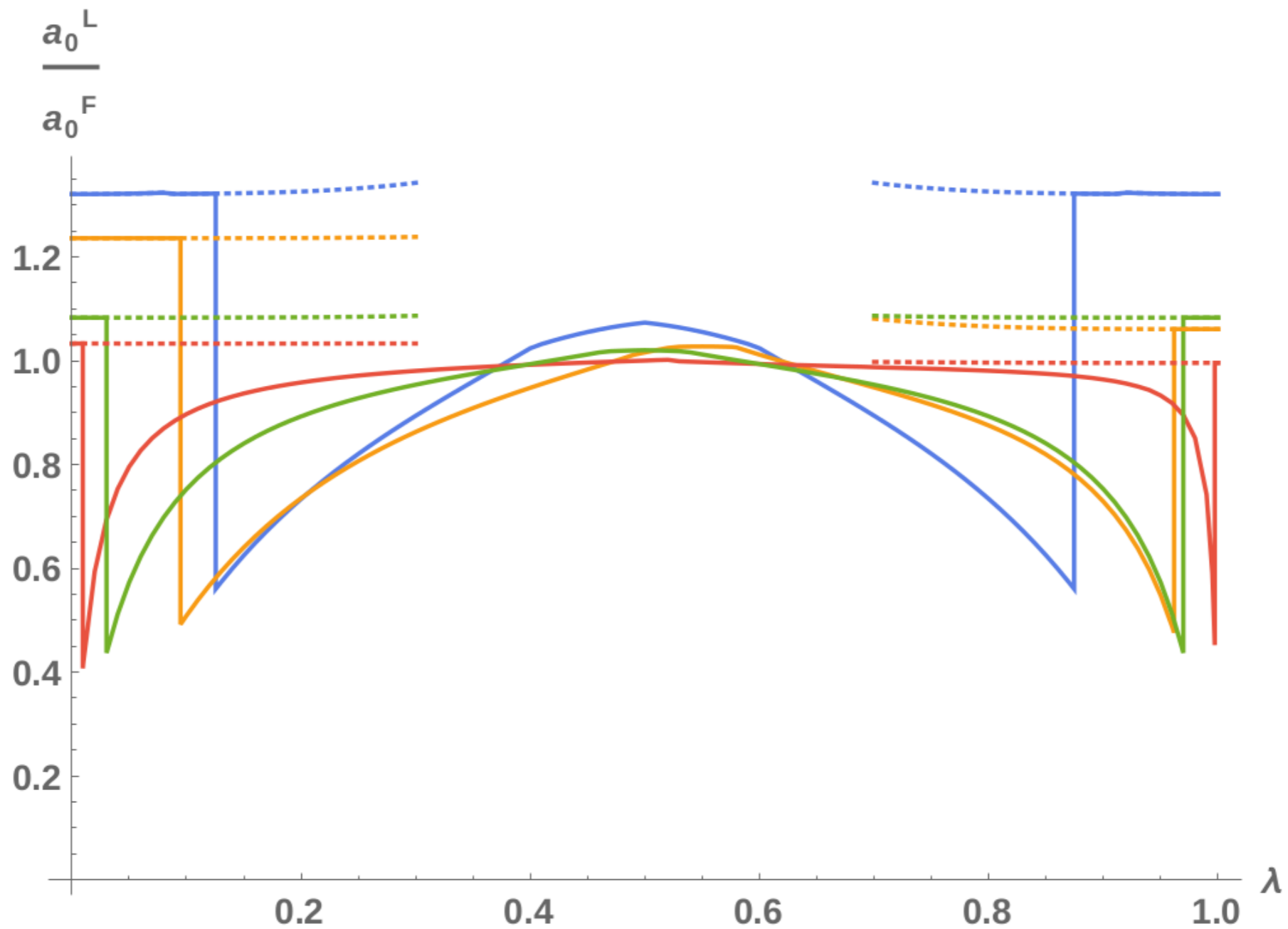
Interesting results?

\exists upper bound on Λ for horizons to exist. Large N , approaches SdS value of $1/9$.

Collective only exists during clustering, for $\lambda \sim 0$ (or 1). Large N , λ_{crit} decreases.

Comparison with FLRW Cosmology

- Scale factors a_0 with structure formation:



Summary and Future Work

- Black hole lattices provide exact analytic test of backreaction.
- Generalised existing models to include Λ and clusters of masses.
- As N increases \rightarrow FLRW.
- Interaction energies appear to be important for masses close together.

Plans:

- Numerically evolve models with Λ .
- Split masses up further to create layers of substructures.



Thank you for listening